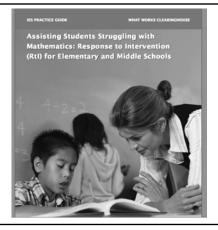
# Response to Instruction and Intervention in Mathematics

A Candid Look at Where We Stand with the Evidence Base

June 15, 2010

#### Overview of Session

- 1. What is a practice guide
- 2. Overview of levels of evidence
- 3. Brief background on RTII
- 4. Highlights on what to teach and how to teach effectively in Tier 2 and Tier 3
  - ✓ Will include Think-Pair-Share activities, so
    - ✓ Pick a partner now



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## Structure of the Practice Guide

- Recommendations
- How to carry out the recommendations
- Levels of evidence
- Potential roadblocks & suggestions

Downloadble for free at IES website (information is on handout)

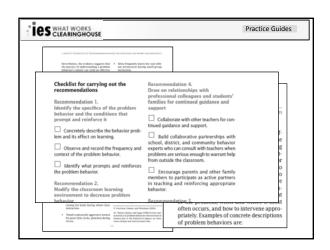
#### The Research Evidence

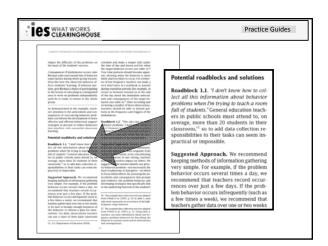
- The panel considered:
  - High quality experimental and quasi-experimental studies.
  - Also examined studies of screening and progress monitoring measures for recommendations relating to assessment.

# **Evidence Rating**

- Each recommendation receives a rating based on the strength of the research evidence.
  - Strong
  - Moderate
  - Low

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#### **Panelists**

- Russell Gersten (Chair), Instructional Research Group (IRG), Professor Emeritus University of Oregon
- Sybilla Beckmann, University of Georgia
- Ben Clarke, Pacific Institute for Research/Instructional Research Group
- Anne Foegen, Iowa State University
- Laurel Marsh, Howard Count Maryland School District
- Jon R. Star, Harvard University
- Bradley Witzel, Winthrop University

## Search for Coherence

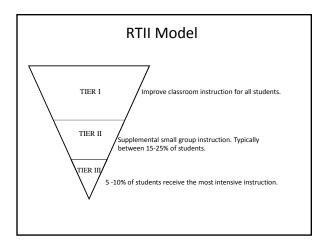
Panel works to develop 5 to 10 assertions that are:

- Forceful and useful
- · And COHERENT
- Do not encompass all things for all people
- Do not read like a book chapter or article
- · Cover grades K-8

#### Challenges for the panel:

- · State of math research
- Paucity of rigorous research on mathematics instruction

Jump start the process by using individuals with topical expertise and complementary views



Moderate  Low  Strong  Strong
Strong
Strong
Moderate
Moderate
Low
Low

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Think Pair Share #1	
Which level of evidence is the	
biggest surprise for you?	
Why?	
	_
Recommendation 1	
Screen all students to identify those at risk	
for potential mathematics difficulties and	
provide interventions to students identified as at risk.	-
Level of Evidence: <b>Moderate</b>	
Evidence	
Technical evidence for validity and reliability of assessments:	
– K-2: Strong	
<ul><li>Grades 3 and up: Limited</li></ul>	

#### Evidence

- Content of Measures
  - Single aspect of number sense (e.g. strategic counting, magnitude comparison) for K/1.
  - For grades 2 and up: Probably measures reflecting major state standards, National Mathematics Panel Benchmarks, Core Standards when they evolve etc. (A lot of work to do here)

<b>Examples of M</b>	issing Num	ber Items
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\_\_\_\_, 20, 21

8, \_\_\_\_, 10

9, 10, \_\_\_\_

# Magnitude Comparison

Which is bigger?

- 11 or 9?
- 79 or 95?
- 19 or 23?


#### Roadblocks

- Screening may identify students as at-risk who do not need services and miss students who do.
- <u>Suggested Approach:</u> Consider delaying screening in kindergarten and first grade until November.

## Roadblocks

- Screening may identify large numbers of students who need support beyond the current resources of the school or district.
- Suggested Approach: Think Pair Share #2

# TIER II & TIER III • Tier II — Is individual or small-group intervention in addition to the time allotted for core mathematics instruction. — Includes curriculum, strategies, and procedures designed to supplement, enhance, and support core classroom instruction. — Can backtrack and/or elaborate/reinforce classroom curriculum. • Tier III — Includes some one-to-one work and more intense methods.


All the following relate to Tier 2 and Tier 3 Participants were students with learning disabilities or problems in learning mathematics Recommendation 2 What to Teach in Intervention Instructional materials for students receiving interventions should focus indepth on: • Whole numbers in kindergarten through grade 6 • Rational numbers in grades 4 through 8 • Applications to geometry and measurement -Level of Evidence: Low Evidence • Consensus across mathematicians, professional organizations, and research panels - National Council Teachers of Mathematics (NCTM) and National Mathematics Advisory Panel (NMAP) - International comparisons - We made the leap to nature of intervention curricula...

#### What to Teach in Intervention (continued)

- Instruction includes:
  - procedures
  - -AND concepts
  - -AND word problems
- Whole number work consistently links operations to number properties

#### **Commutative Property**

- 8 + 7 = 7 + 8
- a + b = b + a

#### Associative

- $9 \times 3 \times 5 = 3 \times 9 \times 5$
- a(bc) = (ab)c

#### Distributive

7(13) = 7(10) + 7(3)

• a(b + c) = ab + ac

#### **Fractions Defined**

- Fractions arise naturally whenever we want to consider one or more parts of an object or quantity that is divided into pieces.
  - − ¼ of a pizza
  - $-\frac{1}{2}$  of the houses in the neighborhood
  - ¾ of a cup of water
- All of these examples use the word of, and all the fractions represent part of some object, collection of objects, or quantity. Source: Beckmann (2008), Mathematics for Elementary Teachers (2nd Ed.)
- Dilemma: how to convey this to kids
- Precursor: teacher must understand all this so that she or he can teach it


#### Recommendation 3

Instruction during the intervention should be **systematic and explicit**. This includes providing models of proficient problemsolving, verbalization of thought processes, guided practice, corrective feedback, and frequent cumulative review.

-Level of Evidence: Strong

#### **Evidence**

- Six randomized controlled trials met standards
- Key themes
  - 1. Extensive practice with feedback
  - 2. Let students provide rationale for their decisions
  - 3. Instructors and fellow students model approaches to problem solving

# Example

• Assignment: Use the lowest common denominator when appropriate

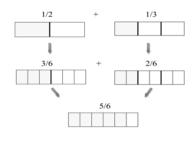
1/2 + 1/3 =

• Student Response

 $\frac{1}{2} + \frac{1}{3} = \frac{2}{5}$ 

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# Explicit instruction helps with understanding of fractions



# **Developing Understanding of Fractions**

• Concrete









Visual





• 0 Partitive model for 3/7



Line model for 4/7 Line model for 3/7 Line model for  $a_7$  . 0  $\frac{3}{7}$  1  $\frac{10}{7}$  2  $\frac{17}{7}$  3

#### Roadblocks

- Intervention curricula may not have explicit instruction and may underestimate the amount of practice and review needed by Tier 2 and Tier 3 students.
- Suggested Approach:
  - 1. Develop guidebooks for school staff to adapt
  - 2. Add new review problems.

#### Recommendation 4

Interventions should include instruction on solving word problems that is based on common underlying structures.

- Level of Evidence: Strong

# Suggestions

- Teach students about the structure of various problem types, how to categorize problems, and how to determine appropriate solutions.
- Middle step –

Is it:

- Quantity (compare)?And/Or
- Change (over time)?

## **Explicitly Teach the Underlying Structure**

- Addition and Subtraction Story Problems
  - Change Problems
    - A quantity is increased or decreased
  - Group Problems
    - Two groups are combined to form a large group
  - Compare Problems
    - $\bullet\,$  Two things are compared to find the difference

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# Change, Group, or Compare?

#### Think Pair Share #3

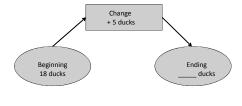
- 1. Dillon leaped 32 inches. Marcus leaped 27 inches. How many more inches did Dillon leap? (Everyday Math 4)
- 2. Uranus has 11 rings. Neptune has 4 rings. How many rings do they have altogether? (sF/AW 3)
- 3. There are 18 ducks. Then 5 more swim over. How many ducks are there now? (Math Expressions 1)

# Change Problems (temporal)

- Sequence
  - Beginning quantity
  - Action quantity is increased or decreased
  - Ending quantity
- Determine whether the change is more or less
  - Begin with quantity increase end up with more
  - Begin with quantity decrease end up with less
- Whether to add or subtract depends on whether there is an increase/decrease *and* which value is missing.

#### Visual Representation for Change Problems

• There are 18 ducks. Then 5 more swim over. How many ducks are there now?



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# Solving similar problems that appear different

- Difficulties encountered by some students
  - Extraneous information
  - Different wording
- Even though the problems have a common underlying structure
- Creates problems for any student who needs intervention

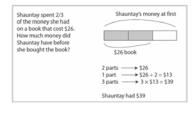
Source: Fuchs et al. (2007

#### Recommendation 5

Intervention materials should include opportunities for the student to work with visual representations of mathematical ideas, and interventionists should be proficient in the use of visual representations of mathematical ideas.

- Level of Evidence: Moderate

Strip diagrams can help students make sense of fractions.

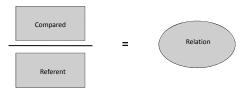


# Suggestions

- Use visual representations such as number lines, arrays, and strip diagrams.
- If necessary consider expeditious use of concrete manipulatives before visual representations. The goal should be to move toward abstract understanding.

# Visual Representation for Multiplicative Compare

• Francine has 5 CDs. Millie has 3 times as many. How many CDs does Millie have? (SF/AW 3)



#### Recommendation 6

Interventions at all grades should devote about 10 minutes in each session to building fluent retrieval of basic arithmetic facts.

- Level of Evidence: Moderate

# Suggestions

- Provide 10 minutes per session of instruction to build quick retrieval of basic facts.
- For student in K-2 grade explicitly teach strategies for efficient counting to improve the retrieval of math facts.
- Teach students in grades 2-8 how to use their knowledge of math properties to derive facts in their heads.

#### Recommendation 7

Monitor the progress of students receiving supplemental instruction and other students who are at risk.

-Level of evidence: Low

#### Evidence

- Non-experimental studies demonstrating the technical adequacy of progress monitoring measures.
- General outcome measures reflecting concepts and computation objectives for the grade level.
- Greater evidence in elementary grades.

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# Suggestions

- Monitor the progress of Tier 2, Tier 3 and borderline Tier 1 students at least once a month using grade appropriate general outcome measures.
- Use curriculum-embedded assessments in intervention materials
  - Frequency of measures can vary every day to once every week.
  - Develop an understanding of their technical characteristics

#### Think Pair Share #4

- How could you develop an understanding of the technical characteristics of curriculum embedded tests?
  - Reliability
  - Are forms equivalent?
  - Who could help?

#### Recommendation 8

Include motivational strategies in tier 2 and tier 3 interventions.

-Level of Evidence: Low

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#### Roadblocks

- Rewards can reduce genuine interest in mathematics by directing student attention to gathering rewards rather than learning math.
- <u>Suggested Approach:</u> Rewards have not shown to reduce intrinsic interest. As students become more successful rewards can be faded so student success becomes an intrinsic reward.

# Questions?

#### Resources

- Center on Instruction (COI)
   <a href="http://www.centeroninstruction.org/resources.cfm?category=math&subcategory=&grade\_start=&grade\_end=#226">http://www.centeroninstruction.org/resources.cfm?category=math&subcategory=&grade\_start=&grade\_end=#226</a>
- National Center for Learning Disabilities (NCLD) RTI Action Network <a href="http://www.rtinetwork.org/">http://www.rtinetwork.org/</a>
- Glover, T. A., & Vaughn, S. (2010). The promise of response to intervention: Evaluating current science and practice. New York: Guilford Press.
- WWC Practice Guide <a href="http://ies.ed.gov/ncee/wwc/publications/practiceguides/">http://ies.ed.gov/ncee/wwc/publications/practiceguides/</a>

Thank you	
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